

第1章 数と式

○ Warm-up の解答

□ 展開

$$(1) (x+2)(x-4) = x^2 + \{2 + (-4)\}x + 2 \cdot (-4) \\ = x^2 - 2x - 8$$

$$(2) (x+1)^2 = x^2 + 2 \cdot x \cdot 1 + 1^2 = x^2 + 2x + 1$$

$$(3) (x+3)(x-3) = x^2 - 3^2 = x^2 - 9$$

□ 因数分解

$$(1) ab - 3ac = a(b - 3c)$$

$$(2) x^2 + 4x + 3 = x^2 + (1+3)x + 1 \cdot 3 = (x+1)(x+3)$$

$$(3) x^2 - 4 = x^2 - 2^2 = (x+2)(x-2)$$

□ 根号を含む式の計算

$$(1) \sqrt{3} \times \sqrt{5} = \sqrt{3 \times 5} = \sqrt{15}$$

$$(2) \frac{\sqrt{6}}{\sqrt{2}} = \sqrt{\frac{6}{2}} = \sqrt{3}$$

$$(3) \sqrt{2} + \sqrt{8} = \sqrt{2} + 2\sqrt{2} = 3\sqrt{2}$$

□ 1次方程式

$$(1) 移項すると \quad 3x = 8 + 4$$

$$\text{すなわち} \quad 3x = 12$$

$$\text{両辺を } 3 \text{ で割って} \quad x = 4$$

$$(2) 移項すると \quad x - 2x = 3 + 6$$

$$\text{すなわち} \quad -x = 9$$

$$\text{両辺に } -1 \text{ を掛けて} \quad x = -9$$

○ 練習の解答

練習 1

(1) 係数 6, 次数 2

(2) 係数 1, 次数 1

(3) 係数 -1, 次数 4

(4) 係数 -3, 次数 3

練習 2

(1) 係数 $2a$, 次数 3

(2) 係数 $3bc^3$, 次数 2

(3) 係数 $-6a$, 次数 3

練習 3

$$(1) 4x^2 + 3x - 1 - 2x^2 - 4x + 6 \\ = (4-2)x^2 + (3-4)x + (-1+6) \\ = 2x^2 - x + 5$$

$$(2) 3a^2 - 2ab - 4b^2 - 5a^2 + 2ab - 8b^2 \\ = (3-5)a^2 + (-2+2)ab + (-4-8)b^2 \\ = -2a^2 - 12b^2$$

練習 4

(1) 3次式

(2) 4次式

練習 5

(1) 3次式, 定数項 $by^2 + c$

(2) 2次式, 定数項 $ax^3 + c$

練習 6

(1) $(a+2)x + (4a^2 - 3a)$

(2) $x^2 + (3y-1)x + (2y^2 - 3y - 2)$

練習 7

$$(1) A + B = (2x^2 + 3x - 1) + (4x^2 - 5x - 6)$$

$$= (2+4)x^2 + (3-5)x + (-1-6) \\ = 6x^2 - 2x - 7$$

$$A - B = (2x^2 + 3x - 1) - (4x^2 - 5x - 6) \\ = 2x^2 + 3x - 1 - 4x^2 + 5x + 6 \\ = (2-4)x^2 + (3+5)x + (-1+6) \\ = -2x^2 + 8x + 5$$

$$(2) A + B = (4x^3 - 3x^2 - 2x + 5) + (2x^3 - 3x^2 + 7) \\ = (4+2)x^3 + (-3-3)x^2 - 2x + (5+7) \\ = 6x^3 - 6x^2 - 2x + 12$$

$$A - B = (4x^3 - 3x^2 - 2x + 5) - (2x^3 - 3x^2 + 7) \\ = 4x^3 - 3x^2 - 2x + 5 - 2x^3 + 3x^2 - 7 \\ = (4-2)x^3 + (-3+3)x^2 - 2x + (5-7) \\ = 2x^3 - 2x - 2$$

練習 8

$$(1) A + 2B = (x^2 + 4x - 3) + 2(2x^2 - x + 4)$$

$$= x^2 + 4x - 3 + 4x^2 - 2x + 8 \\ = (1+4)x^2 + (4-2)x + (-3+8) \\ = 5x^2 + 2x + 5$$

$$(2) 2A - 3B = 2(x^2 + 4x - 3) - 3(2x^2 - x + 4) \\ = 2x^2 + 8x - 6 - 6x^2 + 3x - 12 \\ = (2-6)x^2 + (8+3)x + (-6-12) \\ = -4x^2 + 11x - 18$$

練習 9

$$(1) 2a^3 \times 4a^2 = (2 \times 4) \times a^{3+2} = 8a^5$$

$$(2) a^2 \times (-3a) = -3 \times a^{2+1} = -3a^3$$

$$(3) 4ab^2 \times b^4 = 4 \times a \times b^{2+4} = 4ab^6$$

$$(4) 3x^2y \times (-2x^3y^2) = 3 \times (-2) \times x^{2+3} \times y^{1+2} = -6x^5y^3$$

$$(5) (-a^2b^3)^2 = (-1)^2 \times (a^2)^2 \times (b^3)^2 = a^4b^6$$

$$(6) (-3x^2y)^3 = (-3)^3 \times (x^2)^3 \times y^3 = -27x^6y^3$$

練習 10

$$(1) 4x^2(2x^2 - 3x + 5)$$

$$= 4x^2 \times 2x^2 + 4x^2 \times (-3x) + 4x^2 \times 5$$

$$= 8x^4 - 12x^3 + 20x^2$$